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Fakulteta za matematiko
in fiziko



Jožef Stefan Institute, Ljubljana, Slovenia

quantum computing

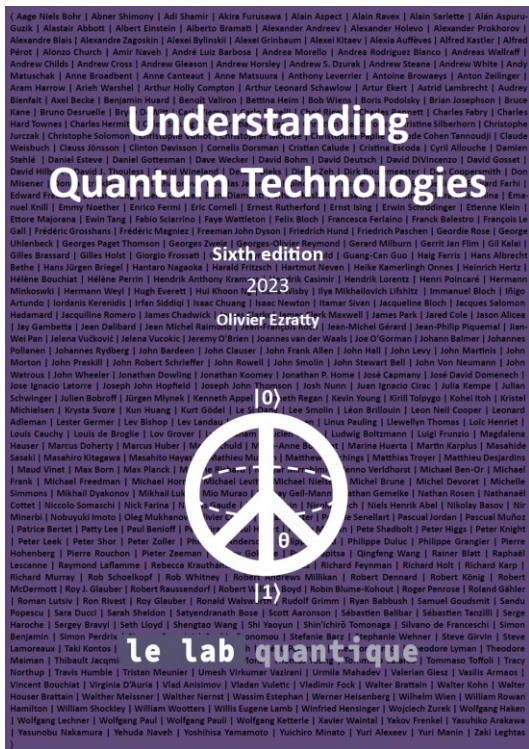
state of the art, challenges, and opportunities

olivier ezratty

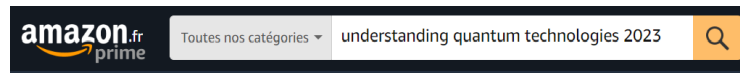
< author | ... >

Ljubljana, April 15th, 2024

olivier@oezratty.net www.oezratty.net @olivez



2023, 1,366 pages
free PDF download

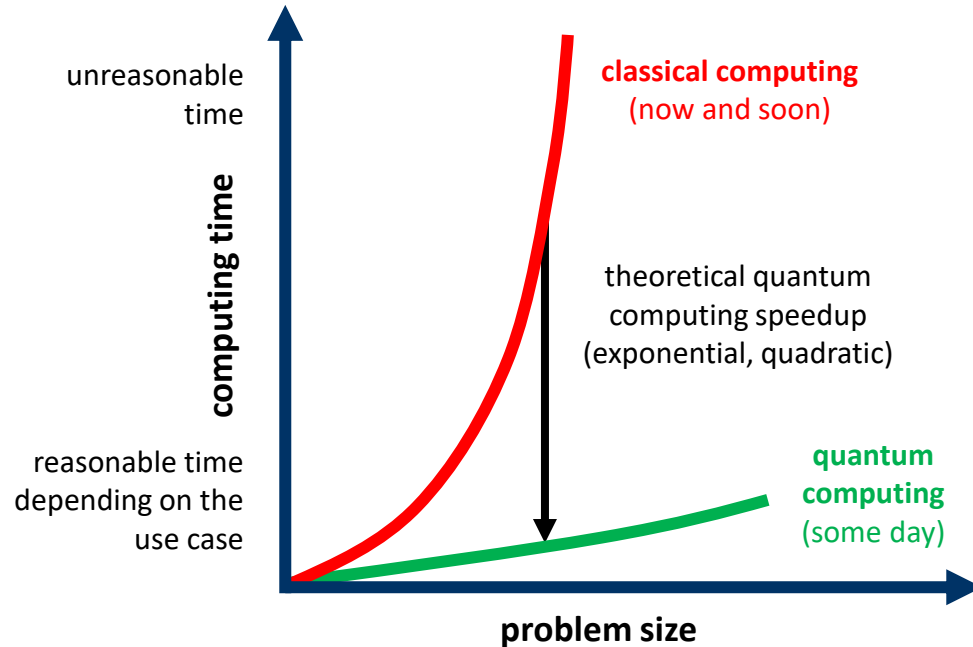


Résultats
En apprendre plus sur ces résultats.

Acheté le oct. 2023	Acheté le oct. 2023	Acheté le oct. 2023
<p>Understanding Quantum Technologies 2023 Volume 1 Édition en Anglais de Olivier Ezratty</p> <p>Broché 24²⁰€</p> <p>Livraison à 0,01€ mercredi 31 janvier dès 35€ d'achat de livres expédiés par Amazon</p>	<p>Understanding Quantum Technologies 2023 Volume 3 Édition en Anglais de Olivier Ezratty</p> <p>★★★★★ ~ 1 Broché 40⁶⁶€</p> <p>Livraison à 0,01€ mercredi 31 janvier</p>	<p>Understanding Quantum Technologies 2023 Volume 2 Édition en Anglais de Olivier Ezratty</p> <p>★★★★★ ~ 1 Broché 40⁶⁶€</p> <p>Livraison à 0,01€ mercredi 31 janvier</p>

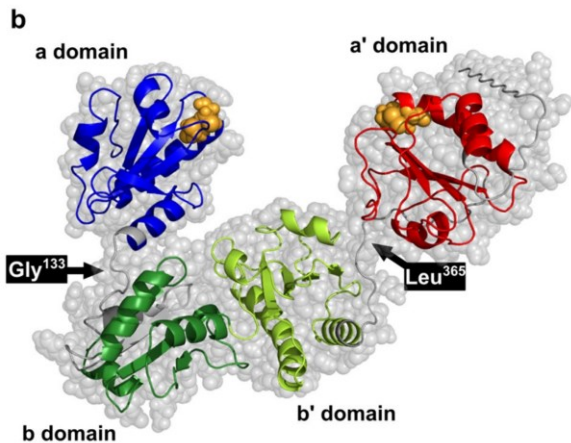
Amazon paperback
edition in 3 volumes

quantum computing *promise*



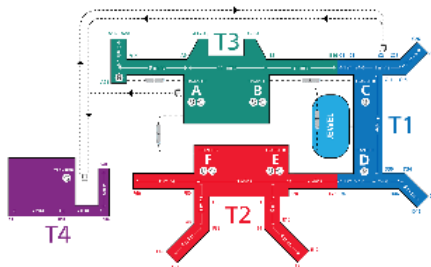
solving
intractable /
exponential
problems in
reasonable time

typical difficult problems

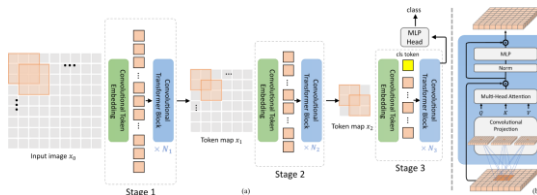


$$i\hbar \frac{\partial \Psi(x,t)}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \Psi(x,t)}{\partial x^2} + V(x)\Psi(x,t)$$

solving Schrodinger's wave equation
to simulate quantum matter



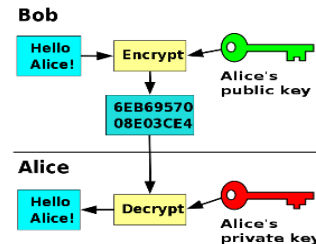
combinatorial optimizations



machine learning
and deep learning

$$\begin{aligned} \frac{\partial^2 u_1}{\partial x_1^2} + \frac{\partial^2 u_2}{\partial x_2 \partial x_1} + \frac{\partial^2 u_3}{\partial x_3 \partial x_1} + \frac{\partial^2 u_1}{\partial x_1^2} + \frac{\partial^2 u_1}{\partial x_2^2} + \frac{\partial^2 u_1}{\partial x_3^2} + f_1 &= 0 \\ \frac{\partial^2 u_1}{\partial x_1 \partial x_2} + \frac{\partial^2 u_2}{\partial x_2^2} + \frac{\partial^2 u_3}{\partial x_3 \partial x_2} + \frac{\partial^2 u_2}{\partial x_1^2} + \frac{\partial^2 u_2}{\partial x_2^2} + \frac{\partial^2 u_2}{\partial x_3^2} + f_2 &= 0 \\ \frac{\partial^2 u_1}{\partial x_1 \partial x_3} + \frac{\partial^2 u_2}{\partial x_2 \partial x_3} + \frac{\partial^2 u_3}{\partial x_3^2} + \frac{\partial^2 u_3}{\partial x_1^2} + \frac{\partial^2 u_3}{\partial x_2^2} + \frac{\partial^2 u_3}{\partial x_3^2} + f_3 &= 0 \end{aligned}$$

solving partial derivative equations



breaking asymmetric
cryptography keys

quantum computing usage categories

research

operations

batteries

drugs

semiconductors

fertilizers production

materials design

condensed matter physics

high-energy particle physics

astrophysics

transportation

financial services

logistics

delivery

energy utilities

telecoms

manufacturing

marketing

quantum & classical computing paradigms

classical computers

quantum inspired

classical algorithms running on classical computer, inspired by quantum algorithms.

classical algorithms improvements



quantum emulators

running quantum computers code on classical computers, for training, debugging and testing

quantum algorithms debug and testing



analog quantum computers

quantum annealing computers

optimization problems and quantum physics simulation



analog quantum simulators



digital quantum computers

gate-based

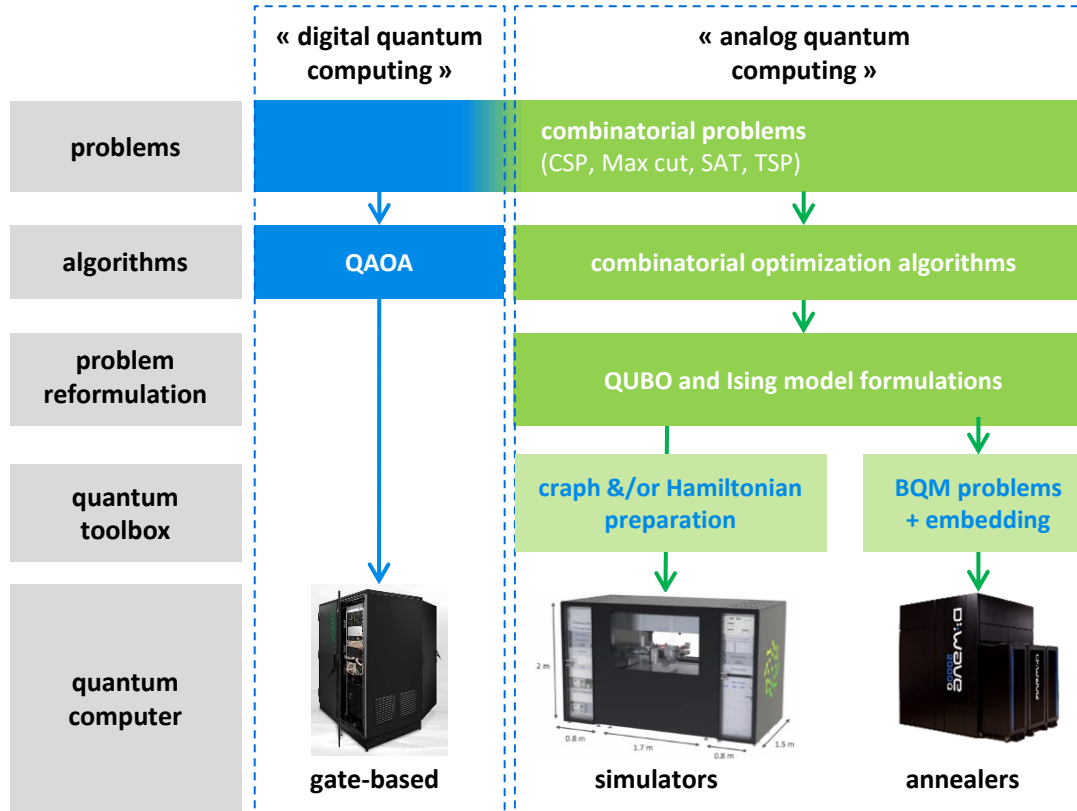
NISQ (Noisy Intermediate Scale Quantum)
no error correction with a few noisy qubits

FTQC (Fault-Tolerant Quantum Computers)
error correction and fault tolerance

general purpose quantum computing, adds search and integer factoring



digital vs analog quantum computing



some mathematical **problem** with data inputs and desired output.

algorithm to solve the given problem, which are mostly hybrid and/or variational.

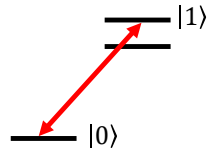
with analog quantum computing, the quantum part of the algorithm may map to a generic QUBO or Ising **model formulation**.

QUBO/Ising model may itself map to a generic problem formulation like **BQM** in the case of D-Wave annealers.

the reformulated problem is **directly solved** by the (analog) quantum computer, in an hybrid manner along with a classical computer.

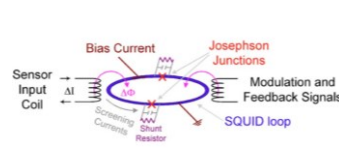
main qubit types

atoms and ions



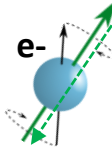
atom energy level

superconducting



loop phase or energy

electron spins



electron spin orientation

photons

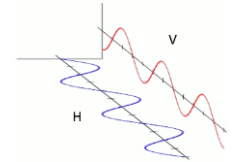
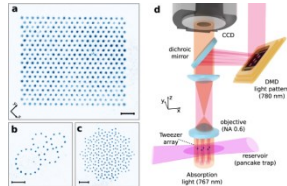


photo polarization (or other property)

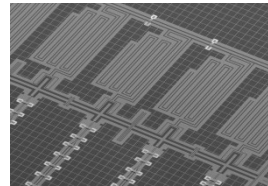
quantum states

physical aspect

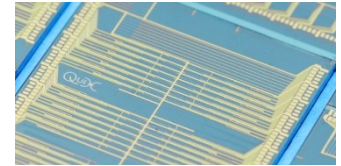
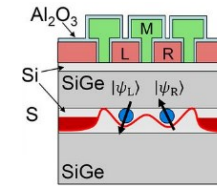
interactions



laser pulses and/or microwaves



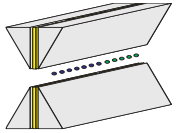
microwave pulses and/or DC current



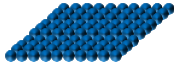
interferometers, polarizing beam splitters, ...

QPUs vendors per qubit type

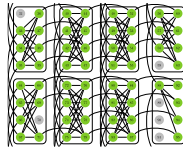
atoms



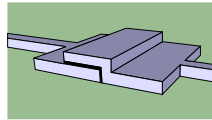
trapped ions



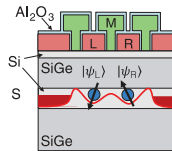
cold atoms



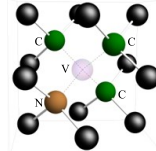
annealing



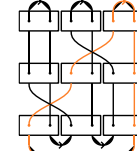
super-conducting



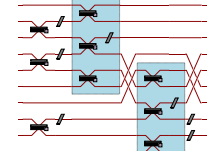
silicon



vacancies



topological



photons

electron superconducting loops & controlled spin

photons



BEN
QUADINAROS



RATTS TYERELL



BOLES ROOR



DUD BOLT



ANAKIN SKYWALKER



MARS GUO



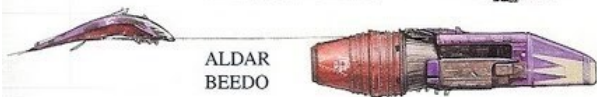
SEBULBA



TEEMTO PAGALIES



ALDAR
BEEDO



NEVA KEE



GASGANO



ARK "BUMPY" ROOSE



ODY MANDRELL



ELAN MAK



EBE ENDOCOTT



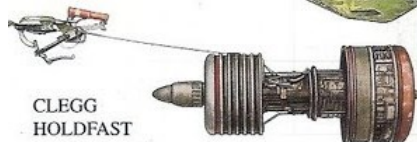
MAWHONIC



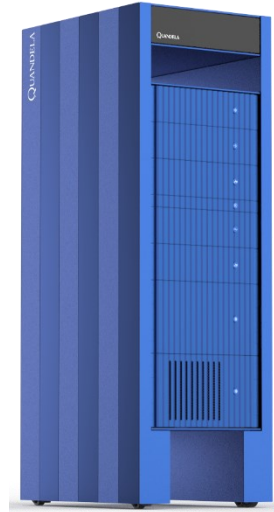
WAN
SANDAGE



CLEGG
HOLDFAST



IBM



QUANDELA



IONQ



PASQAL



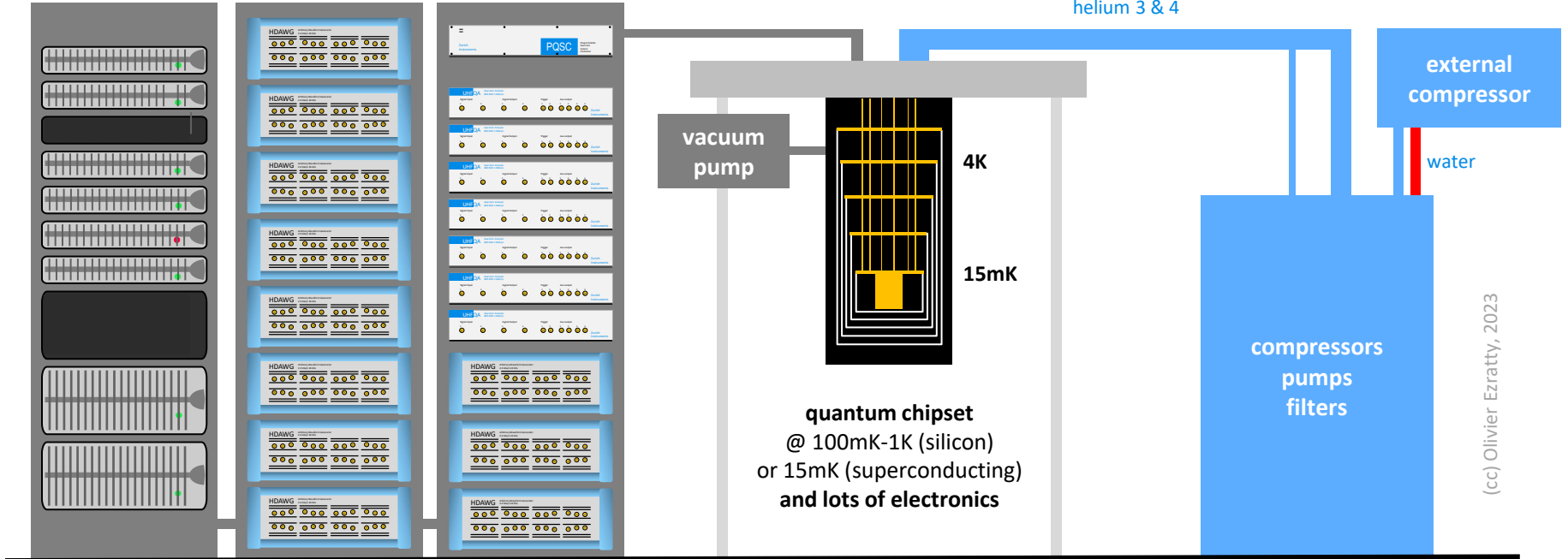
inside a typical quantum computer

computing
servers, network,
software, data

qubits control electronics
microwave generators, readout
systems and various electronics

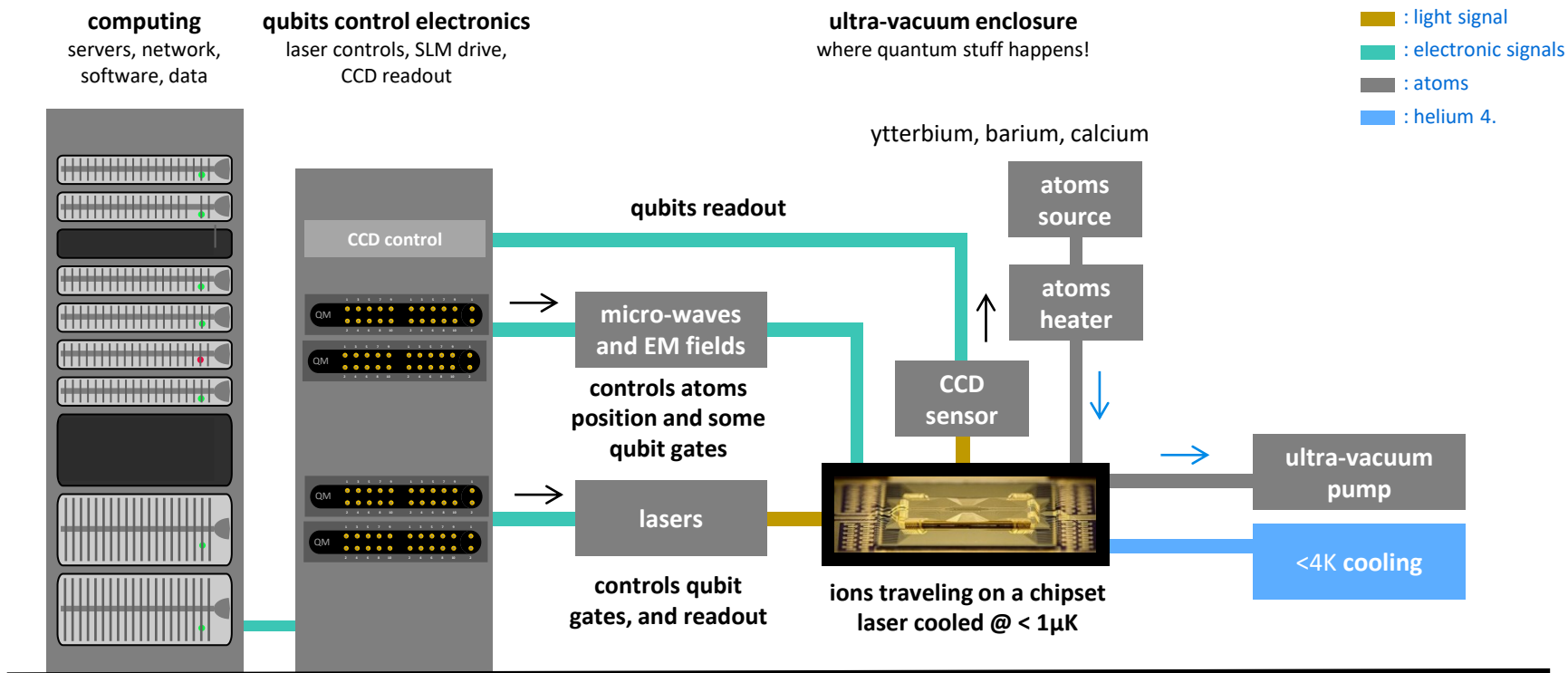
« chandelier » in cryostat
where quantum stuff happens!

cryogenic installation
helium 3 & 4
gas pumps and compressor



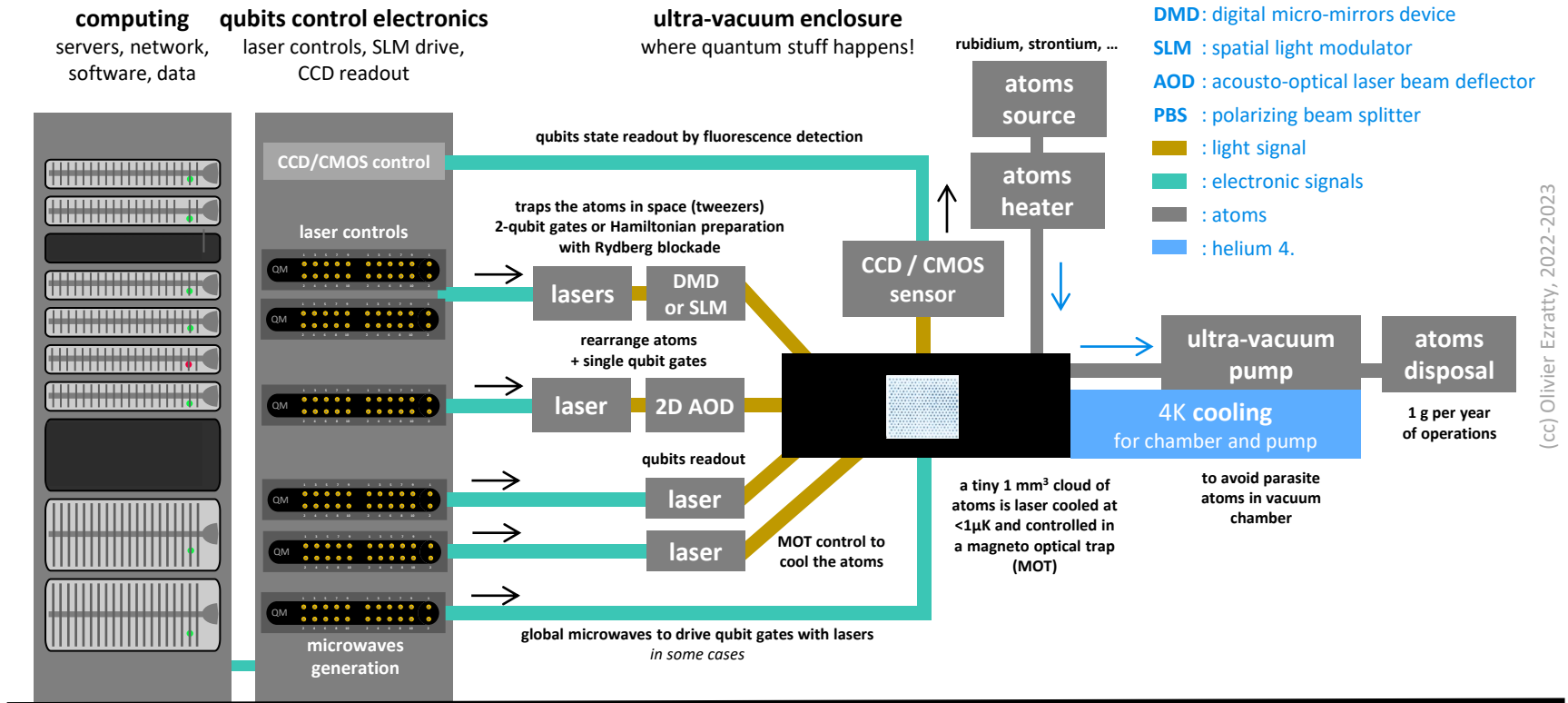
for superconducting or electron spin qubits

inside a trapped ions QC



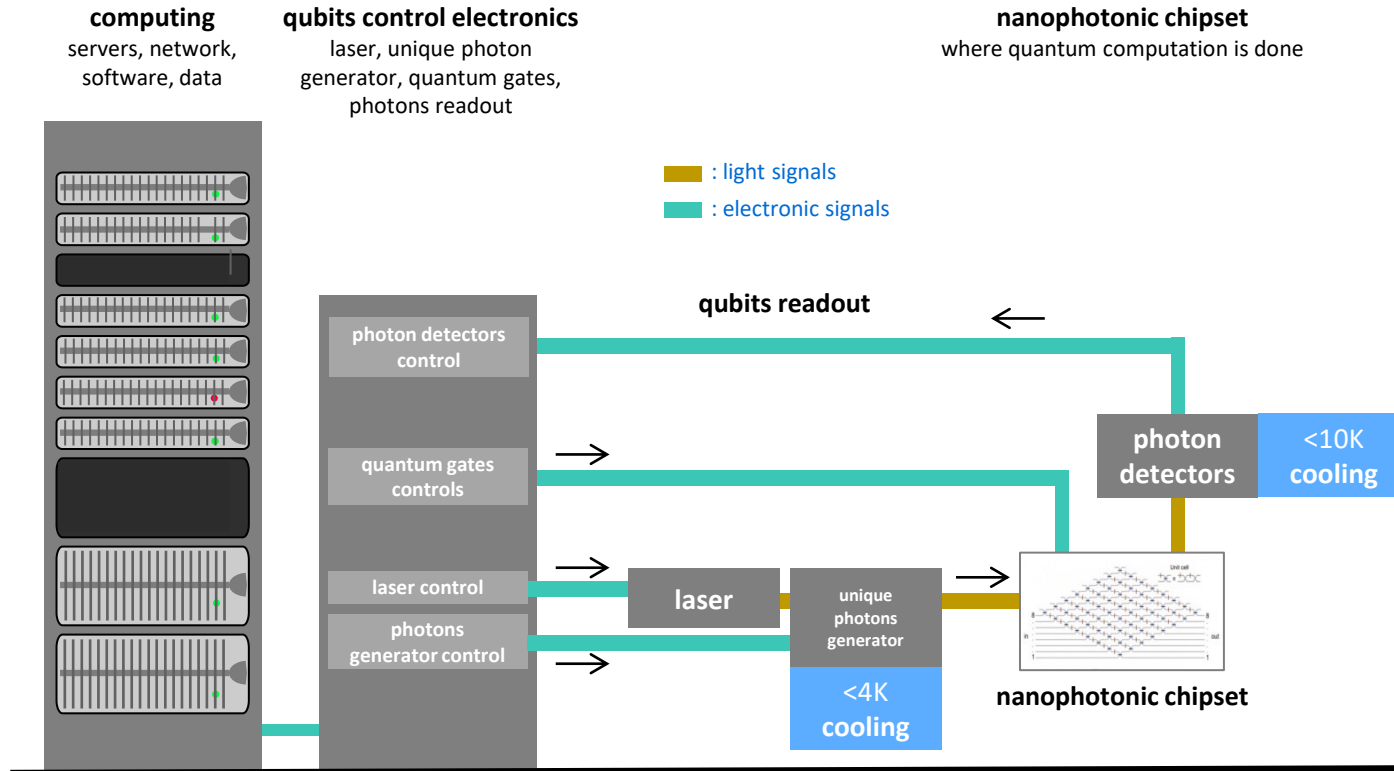
IonQ trapped ions case

with a neutral atoms quantum computer



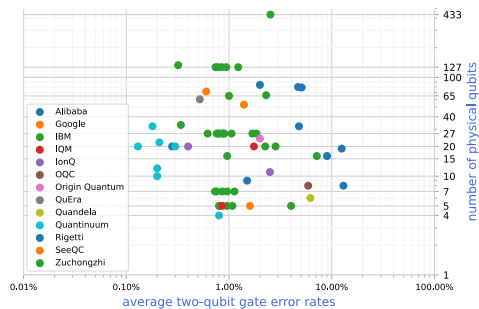
(cc) Olivier Ezratty, 2022-2023

with a photon qubits quantum computer

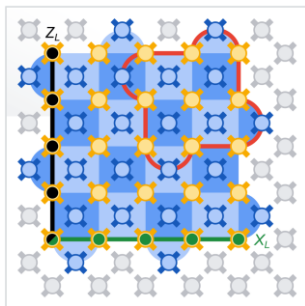


Quandela case

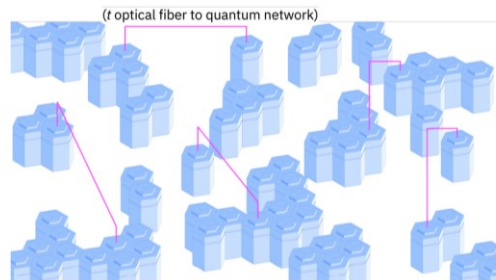
key QPU challenges



qubits fidelities

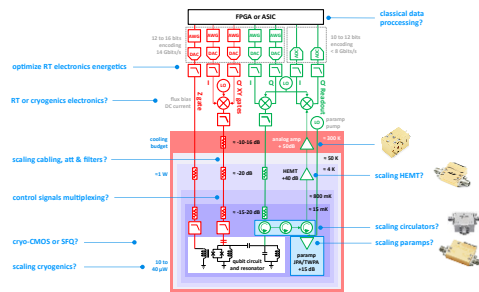


errors mitigation and correction

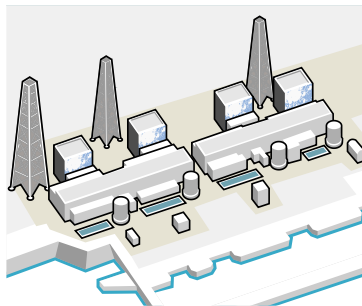


(e) type modularity involves microwave-to-optical transduction to link QPUs in different dilution refrigerators.

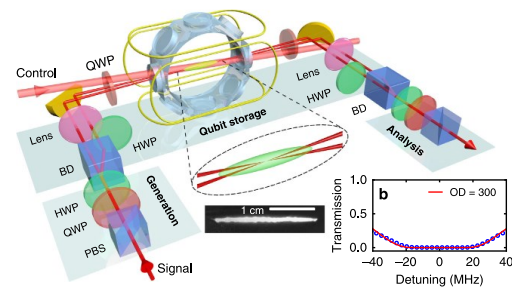
quantum interconnect



enabling technologies scalability

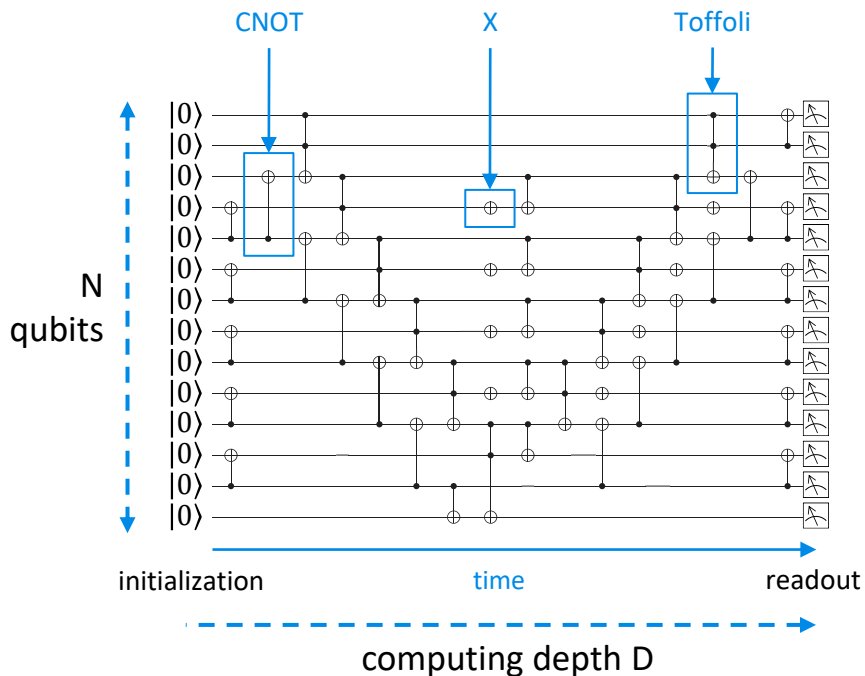


energy consumption



quantum memory

raw algorithm fidelities requirements



$$\text{desired error rate} < \frac{1}{N \times D}$$

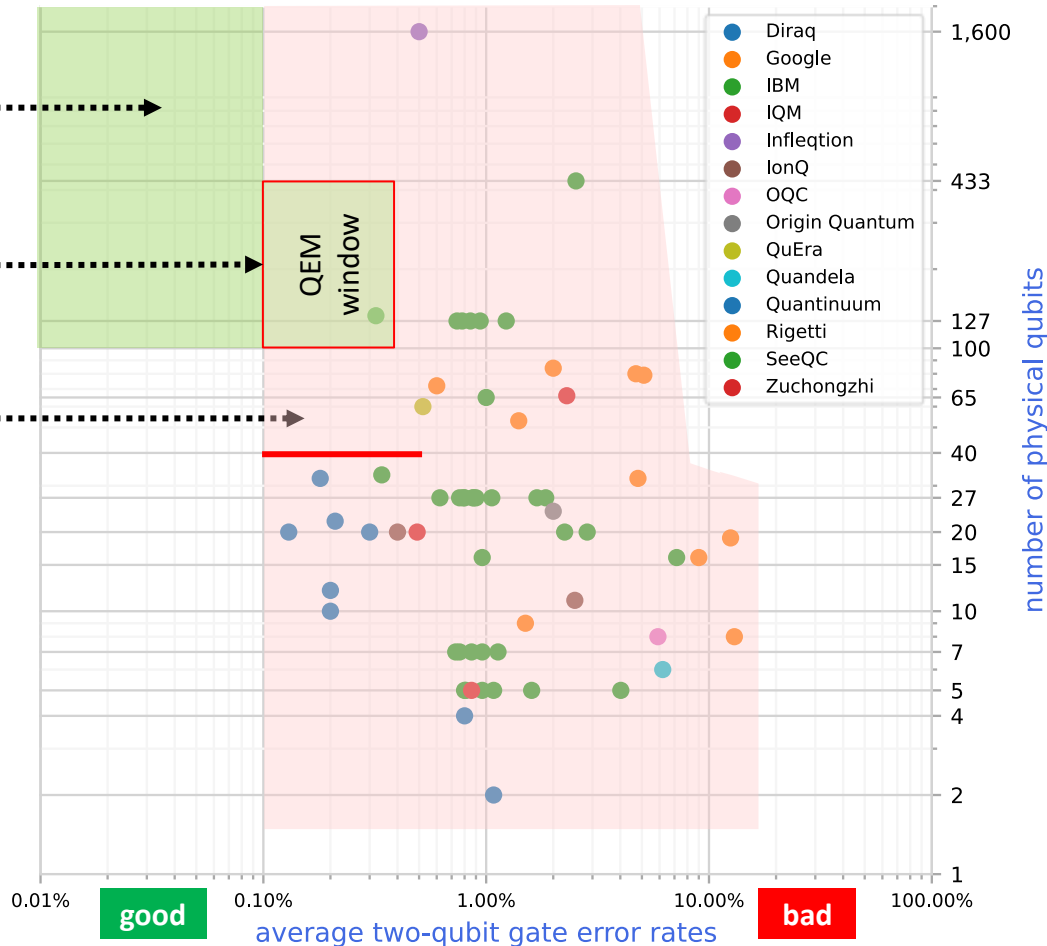
N qubits	D depth	required error rate (%)	required fidelity (%)	available fidelity (%)
50	100	0.02000%	99.98%	99.30%
133	300	0.00251%	99.9975%	99.6%
433	1000	0.00023%	99.9998%	98%
1121	2000	0.00004%	99.99996%	N/A

but... QEC cost discrepancy between Clifford and non-Clifford gates

useful NISQ*
 requirements

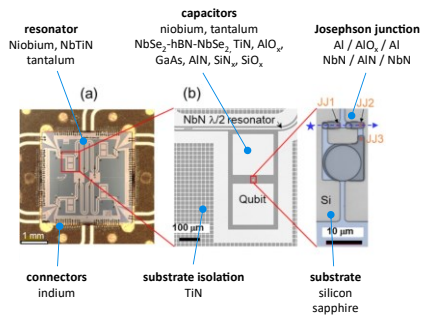
with quantum
 error mitigation

state of the art
 easy to emulate classically,
 too noisy to be useful

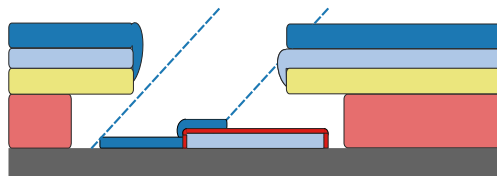


* NISQ = noisy intermediate scale quantum computers.

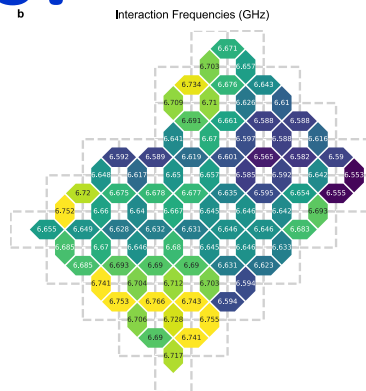
how to improve qubit fidelities? *



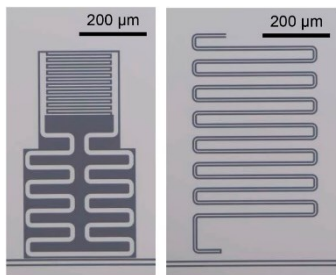
materials



manufacturing



reduce crosstalk



tune qubit parameters

Cross-Cross Resonance Gate

Kentaro Heya^{1,2,*} and Naoki Kanazawa^{1,†}

¹IBM Quantum, IBM Research Tokyo, 19-21 Nihonbashi Hakozaki-cho, Chuo-ku, Tokyo 103-8510, Japan

²Research Center for Advanced Science and Technology (RCAST), The University of Tokyo, Meguro-ku, Tokyo 153-8904, Japan

High-fidelity three-qubit *i*Toffoli gate for fixed-frequency superconducting qubits

Yosep Kim,^{1,*} Alexis Morvan,¹ Long B. Nguyen,¹ Ravi K. Naik,^{1,2} Christian Jünger,¹

Larry Chen,² John Mark Kreikebaum,^{2,3} David I. Santiago,^{1,2} and Irfan Siddiqi^{1,2,3}

¹Computational Research Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

²Department of Physics, University of California, Berkeley, California 94720, USA

³Materials Science Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

(Dated: December 21 2022)

use different primary gates



improve control signals quality

* using here the example of superconducting qubits

logical qubits and FTQC

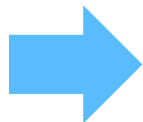
physical qubit

error rates $\approx 0.1\%$

+

error correction code

threshold, physical qubits overhead,
connectivity requirements, syndrome
decoding and scale

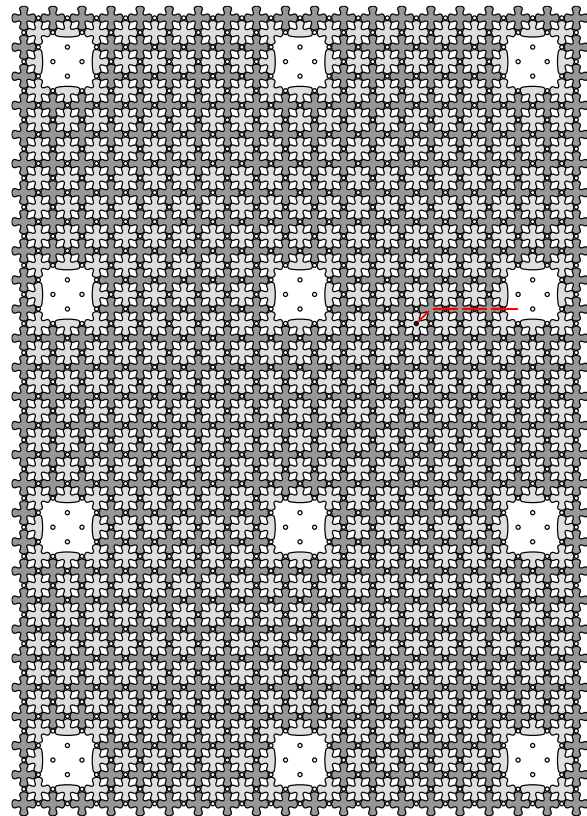
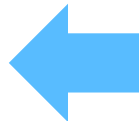


logical qubit

error rate $< 10^{-8}$ to $< 10^{-15}$

fault tolerance

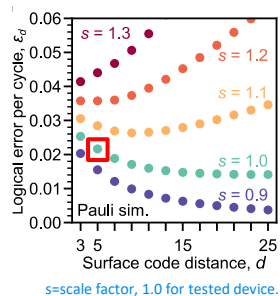
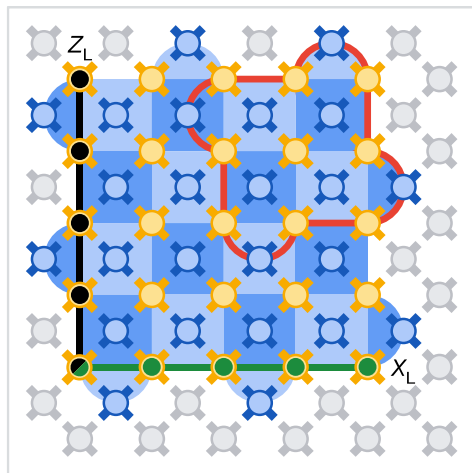
avoid error propagation and amplification
implement a universal gate set
fault-tolerant results readout



tens to thousands qubits

<https://arxiv.org/abs/1202.2639>

existing logical qubits *above* break-even

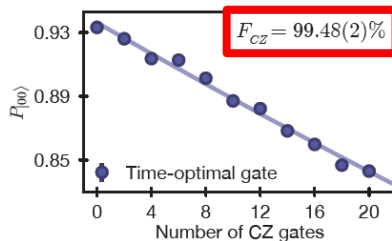


- Data qubit (d^2)
- Measure qubit ($d^2 - 1$)
- Unused
- Subset distance-3

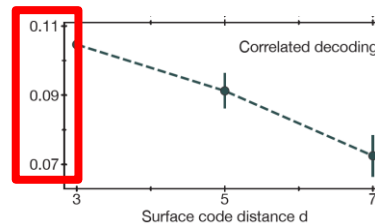
Sycamore 72-qubit processor
single distance-5 logical qubit – July 2022

it slightly outperforms a distance-3 logical qubit
 but with providing a higher error rate (2.1%)
 than the underlying physical qubits (0.7%).

physical fidelities



logical error



Harvard-MIT-QuEra 48 logical qubits –
December 2023

logical 2-qubit gate error rates at 7%
 with distance-7 surface code while
 physical qubit error rate is 0.5%.

Microsoft-Quantinuum logical qubits

Demonstration of logical qubits and repeated error correction with better-than-physical error rates

M. P. da Silva,¹ C. Ryan-Anderson,² J. M. Bello-Rivas,¹ A. Chernoguzov,² J. M. Dreiling,² C. Foltz,² J. P. Gaebler,² T. M. Gatterman,² D. Hayes,² N. Hewitt,² J. Johansen,² D. Lucchetti,² M. Mills,² S. A. Moses,² B. Neyenhuis,² A. Paz,¹ J. Pino,² P. Siegfried,² J. Strabley,² S. J. Wernli,¹ R. P. Stutz,² and K. M. Svore¹

¹Microsoft Azure Quantum
²Quantinuum

(Dated: April 2, 2024)

The promise of quantum computers hinges on the ability to scale to large system sizes, e.g., to run quantum computations consisting of more than 100 million operations fault-tolerantly. This in turn requires suppressing errors to levels inversely proportional to the size of the computation. As a step towards this ambitious goal, we present experiments on a trapped-ion QCCD processor where, through the use of fault-tolerant encoding and error correction, we are able to suppress logical error rates to levels below the physical error rates. In particular, we entangled logical qubit states encoded in the $[[7, 1, 3]]$ code with error rates $9.8\times$ to $500\times$ lower than at the physical level, and entangled logical qubit states encoded in a $[[12, 2, 4]]$ code with error rates $4.7\times$ to $800\times$ lower than at the physical level, depending on the judicious use of post-selection. Moreover, we demonstrate repeated error correction with the $[[12, 2, 4]]$ code, with logical error rates below physical circuit baselines corresponding to repeated CNOTs, and show evidence that the error rate per error correction cycle, which consists of over 100 physical CNOTs, approaches the error rate of two physical CNOTs. These results signify an important transition from noisy intermediate scale quantum computing to reliable quantum computing, and demonstrate advanced capabilities toward large-scale fault-tolerant quantum computing.

<https://arxiv.org/abs/2404.02280>

claim: logical qubit with x800 improvement vs physical qubit

reality: x800 improvement only for the first gate cycle!

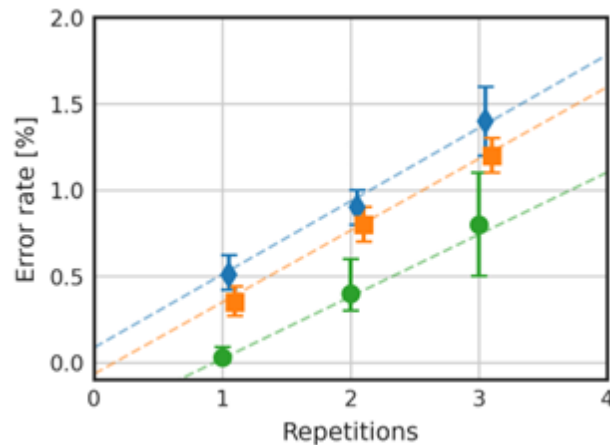
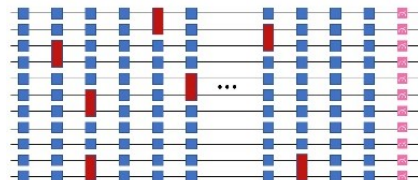
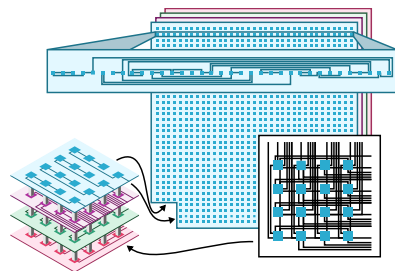
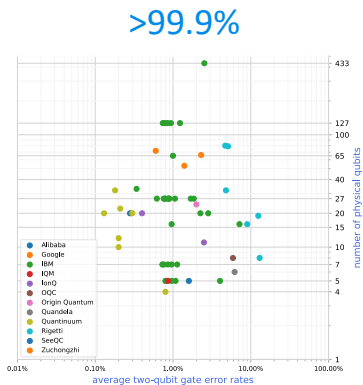


FIG. 7. Observed error rate for circuits with 1 to 3 rounds of error correction with the $[[12, 2, 4]]$ Carbon code (green circles) and physical baselines (blue diamond for pairs of 1-bit teleportations, and orange squares for pairs of CNOTs). Results are offset along the x-axis for clarity. Linear fits are obtained by maximum-likelihood estimation (see Appendix A for details).

Craig Gidney's comment on Scott Aaronson's blog

<https://scottaaronson.blog/?p=7916#comment-1973425>

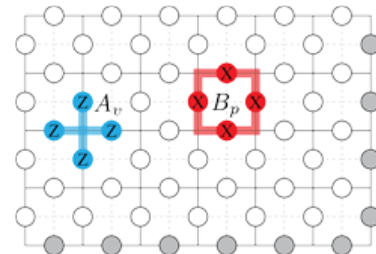
qubits for FTQC?



algorithm breadth and depth

$n_T = \# \text{ of T gates in algorithm}$

logical qubit error rate $< \frac{1}{n_T}$



physical qubits fidelities

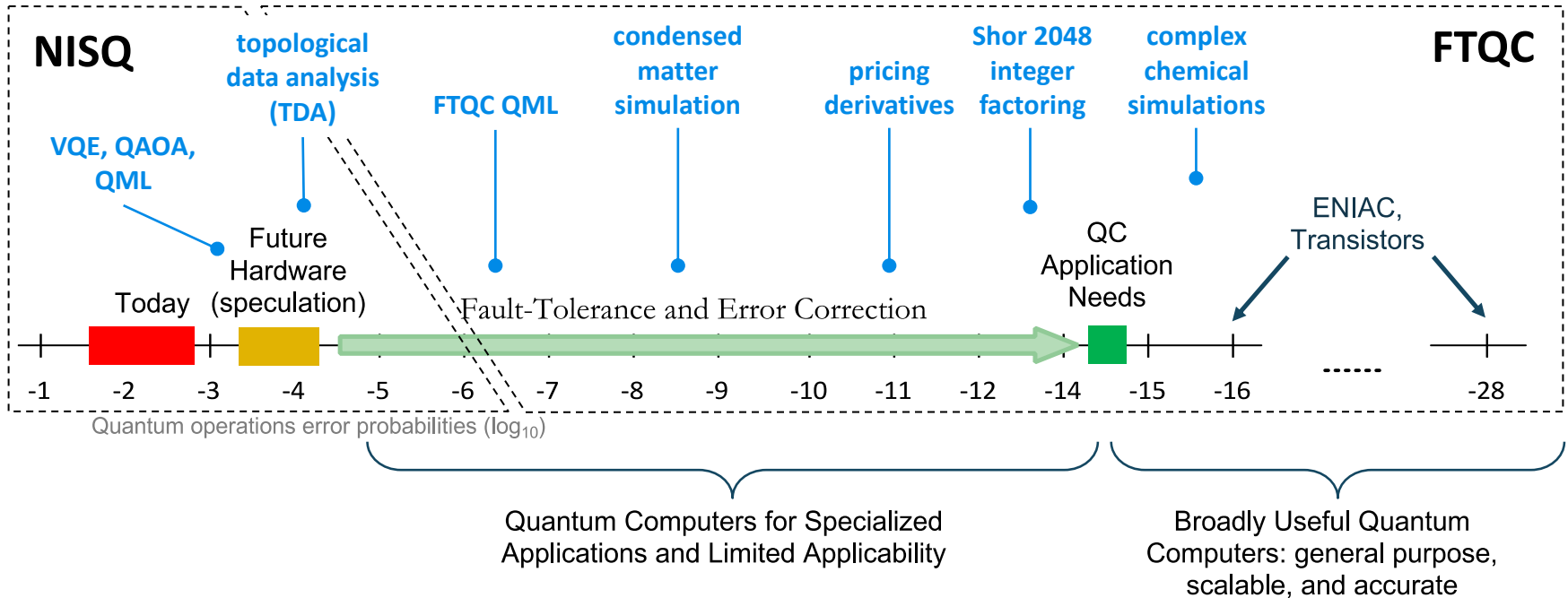
physical qubits connectivity

error correction code

physical qubits / logical qubit

dynamically adjusted against the algorithm size

logical qubits requirements



source: How about quantum computing? by Bert de Jong, DoE Berkeley Labs, June 2019 (47 slides) + Olivier Ezratty additions, 2021-2024.

Li-Ion battery chemical simulation

PHYSICAL REVIEW A **106**, 032428 (2022)

needs...

6,652 logical qubits

10^{-12} error rate

computing times in months/years



source: Simulating key properties of lithium-ion batteries with a fault-tolerant quantum computer by Alain Delgado et al, April-September 2022 (31 pages).

Simulating key properties of lithium-ion batteries with a fault-tolerant quantum computer

Alain Delgado^{1,*}, Pablo A. M. Casares^{2,*}, Roberto dos Reis^{1,3}, Modjtaba Shokrian Zini,¹ Roberto Campos^{2,4}, Norge Cruz-Hernández⁵, Arne-Christian Voigt,⁶ Angus Lowe,¹ Soran Jahangiri,¹ M. A. Martin-Delgado^{2,7}, Jonathan E. Mueller⁶, and Juan Miguel Arrazola^{1,†}

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²Departamento de Física Teórica, Universidad Complutense de Madrid, 28040 Madrid, Spain


³Department of Materials Science and Engineering, Northwestern University, Evanston, Illinois 60208, USA

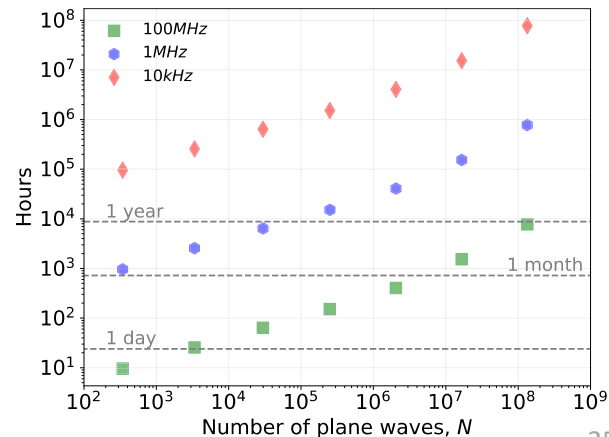
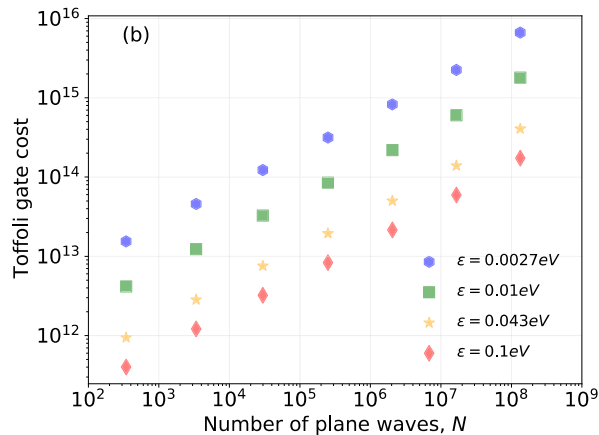
⁴Quasar Science Resources SL, 28231, Las Rozas de Madrid, Spain

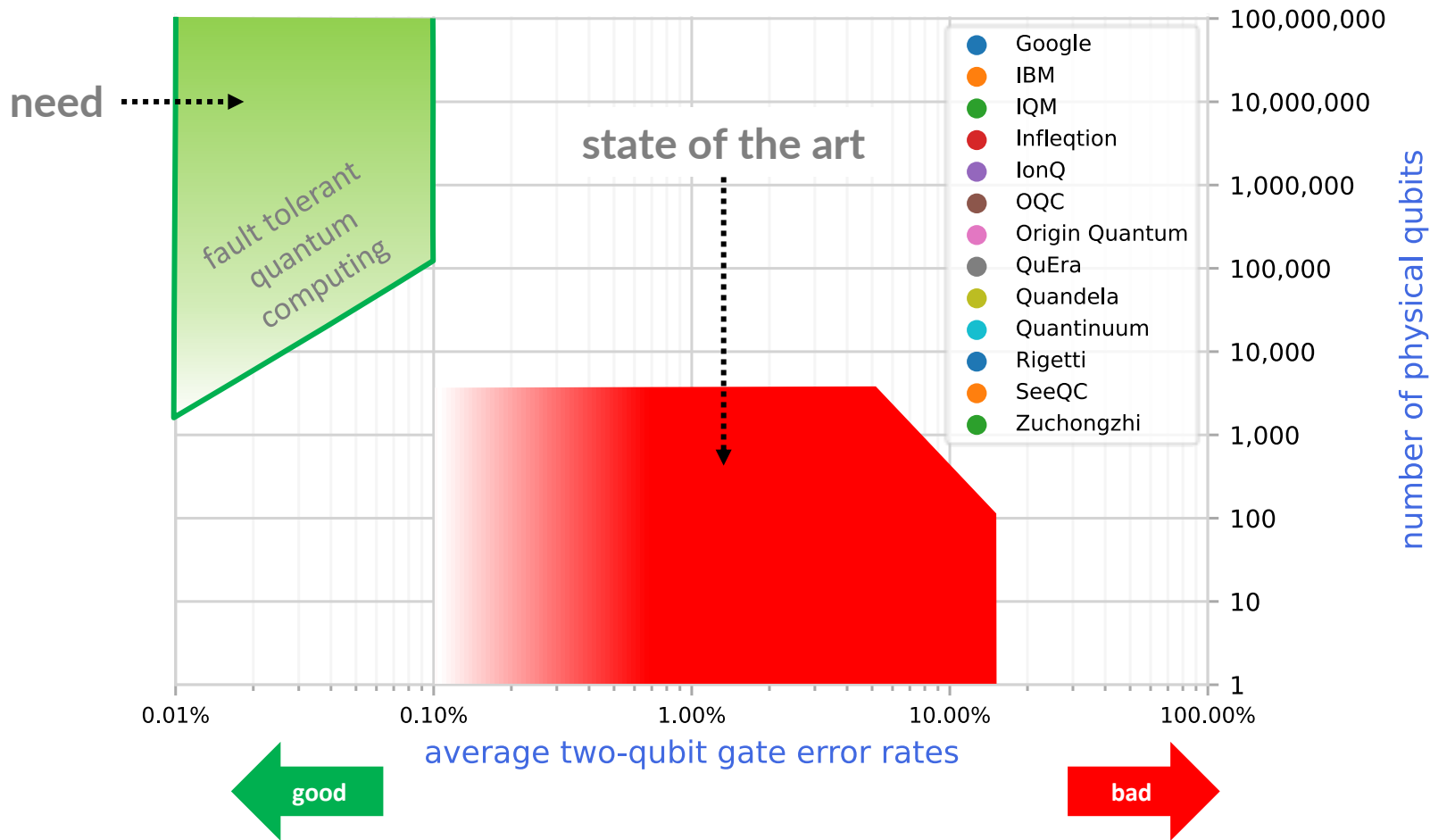
⁵Departamento de Física Aplicada I, Escuela Politécnica Superior, Universidad de Sevilla, Sevilla, E-41011, Spain

⁶Volkswagen AG, Berliner Ring 2, 38440 Wolfsburg, Germany

⁷CCS-Center for Computational Simulation, Universidad Politécnica de Madrid, 28040 Madrid, Spain

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some hardware scalability challenges and trade-offs

the superconducting qubit case

optimize RT electronics energetics

RT or cryogenics electronics?

scaling cabling, att & filters

control signals multiplexing

cryo-CMOS or SFQ electronics?

at which temperature?

long range qubit connectivity

scaling cryogenics

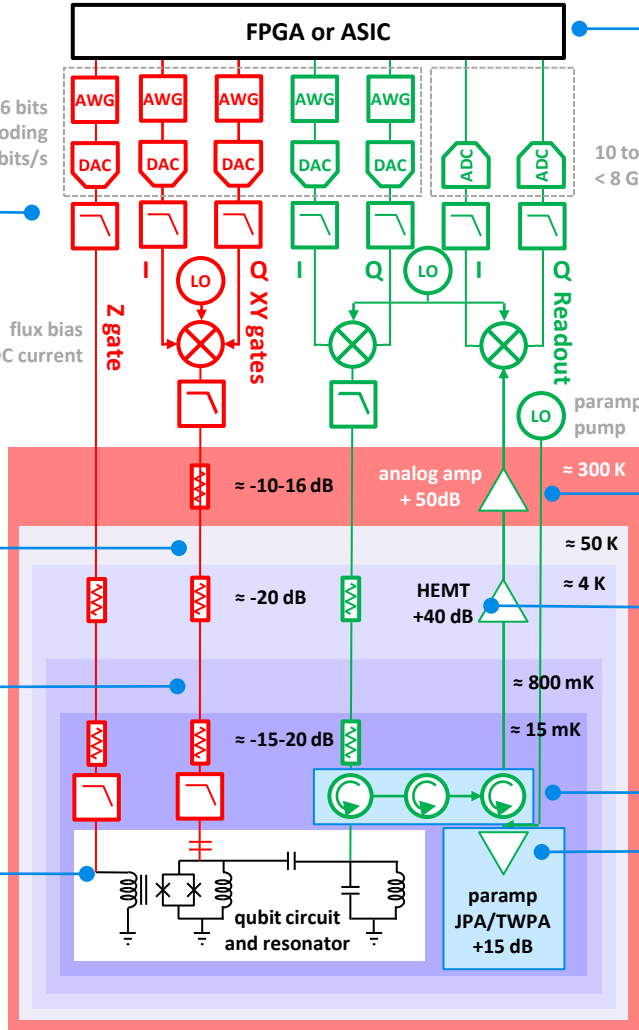
12 to 16 bits encoding
14 Gbits/s

flux bias
DC current

cooling budget

≈ 1 W

10 to 40 μW



FPGA or ASIC

AWG

AWG

AWG

AWG

AWG

DAC

DAC

DAC

DAC

DAC

ADC

ADC

Z gate

XY gates

Q

I

Q Readout

param pump

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error syndrome decoding
error correction codes

10 to 12 bits encoding
< 8 Gbits/s

QPU interconnect

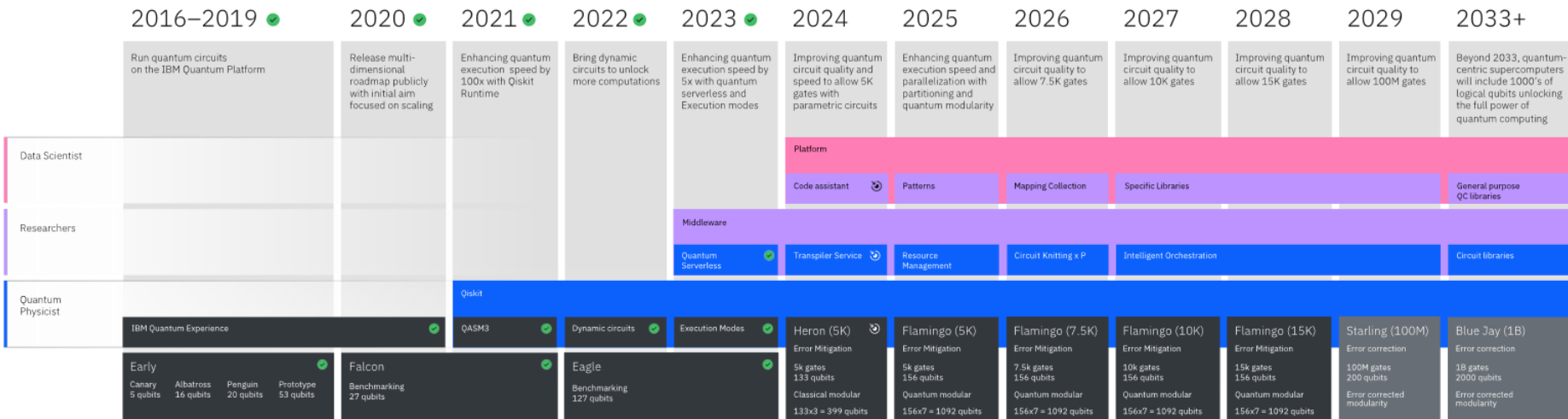
scaling HEMTs

scaling circulators

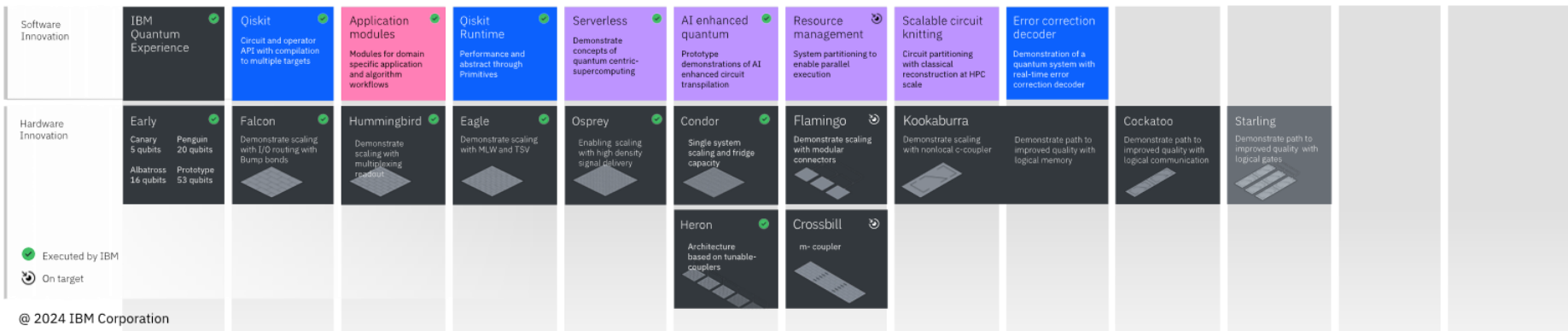
scaling paramps

qubit fidelities improvement





Innovation Roadmap



Executed by IBM

On target



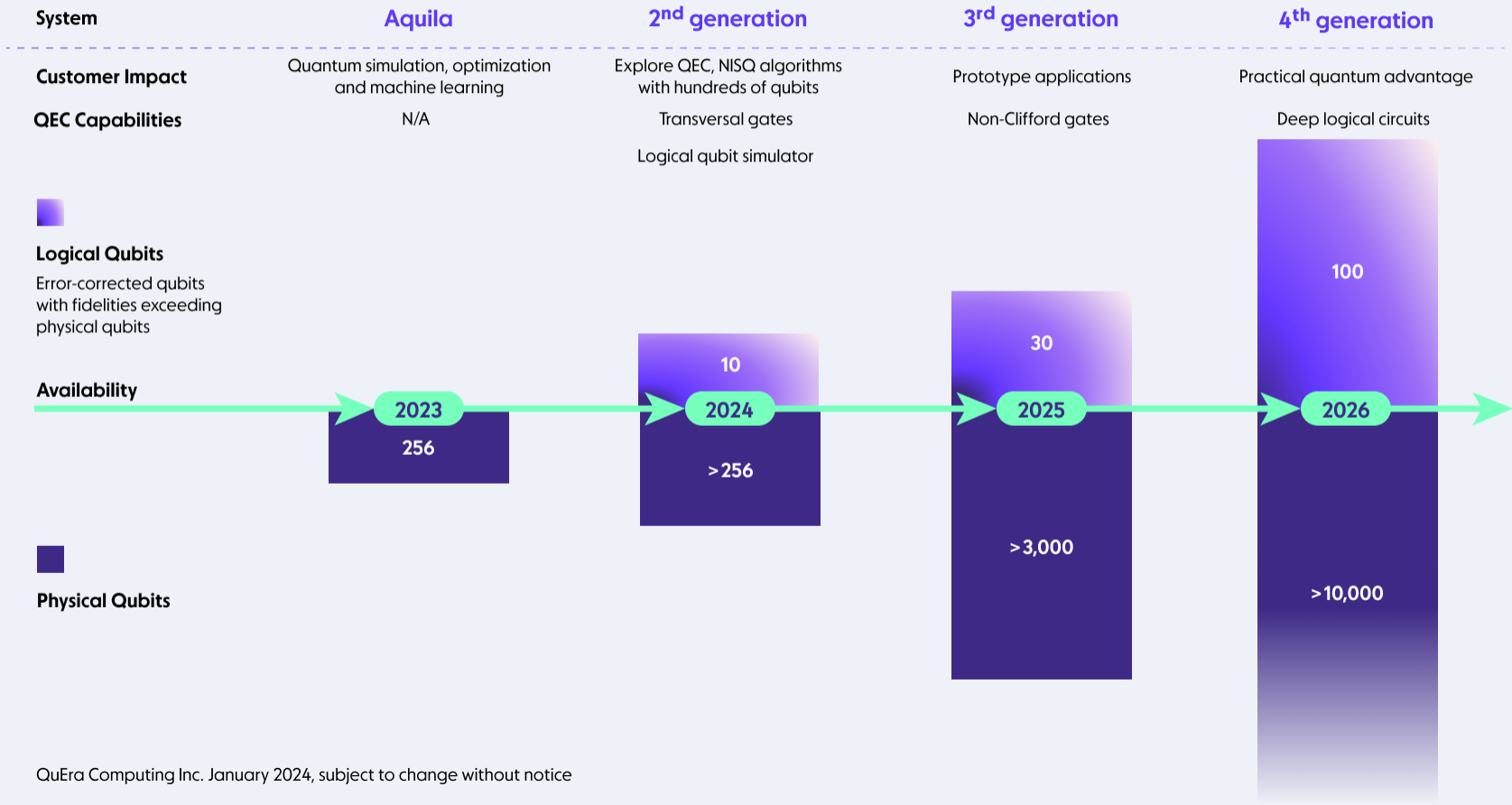
IBM Quantum System 2 with three Heron 133-qubit QPUs

Unlocking True Commercial Advantage

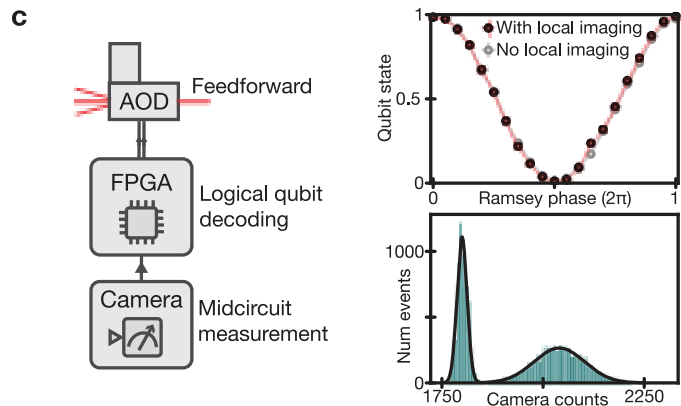
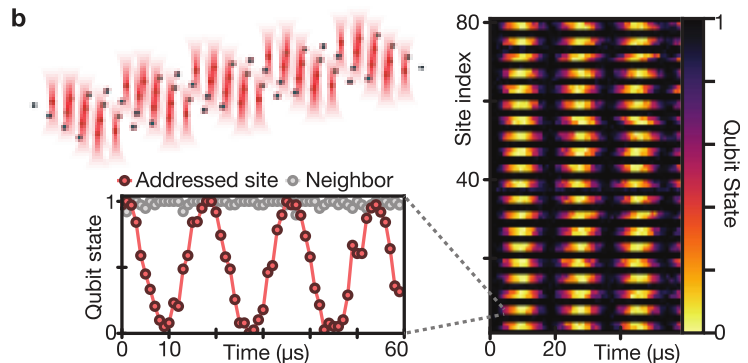
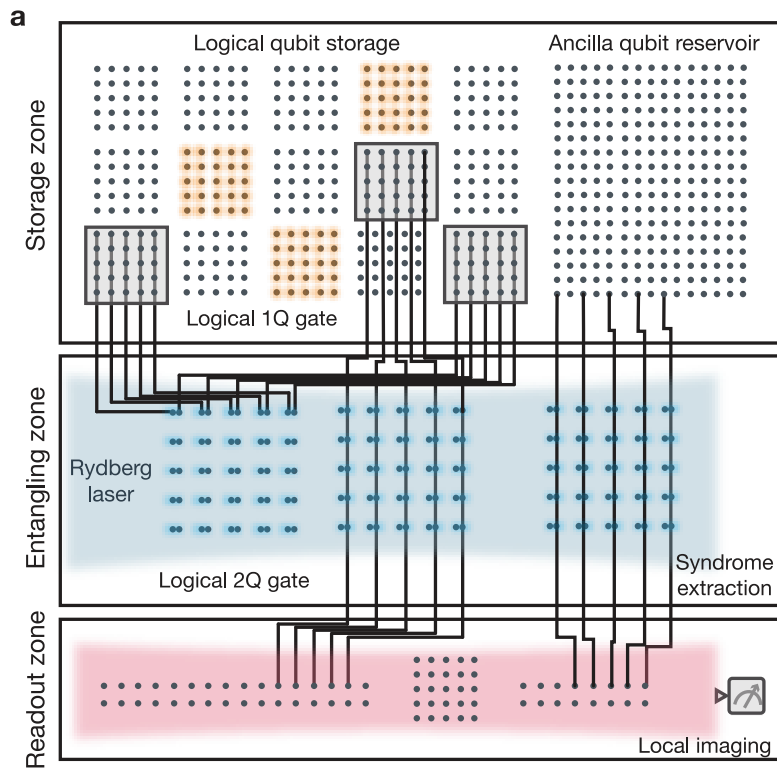
Designing data center ready solutions at scale

	2024 Error Detection	2026 Error Correction	2028 Commercial Advantage
Logical Performance	Dual-species crosstalk-free measurement	Logical circuit depth > 1,000 Universal quantum gate set	Logical circuit depth > 1 million.
Logical Qubits	2	>10	>100
Logical Operations Rate		10,000/sec	100,000/sec
Physical qubits	1,600	8,000	40,000
Fidelity	2Q (cz): Local IQ: Global IQ:	99.50% 99.90% 99.99%	99.90% 99.95% 99.99%
Software	Tooling (qcvv) for verifying fault-tolerant properties	Optimized compilation of fault-tolerant circuits	Exponential speedup demonstration
Enabling technologies	Optimized laser pulse modulation	Advanced photonic beam steering	Realtime atom reloading

Error-Corrected Quantum Computing Roadmap



Harvard / QuEra logical qubits



source: Logical quantum processor based on reconfigurable atom arrays by Dolev Bluvstein, Mikhail D. Lukin et al, December 2023 (32 pages).

Technology
PASQAL & affiliated ecosystem

Products

	2022 - 2023	2024 - 2025		2026 - 2027		2028+
HARDWARE PLATFORM						
Max qubits	200	1,000		10,000		
Addressability	Z add	Z+X add	Addressable 1Q and 2Q gates			
Base repetition rate	1 Hz	3 Hz		10 Hz		100 Hz
FTQC Program		Atom shuttling	Ultra High-Fidelity Gates	Scalable logical qubits architecture		
HARDWARE ACCELERATED LIBRARIES						
Quantum Matter & Quantum AI	Algorithm Blueprint	Algorithm Development		Production		
QUANTUM PROCESSORS						
Generation	Orion Alpha ~3M gates	Orion Beta ~5M gates On premise delivery	Orion Gamma ~10M gates On premise delivery	Vela ~40M gates	Pegasus ~200M gates	Centaurus FTQC QPU 128+ Logical qubits 200M+ gates
Total hours of QPU for users	500	5-10,000	20-30,000	60-70,000	200-250,000	500-550,000
Factories	France	Canada	Factory 3			
COMMUNITY						
Platform		Learn	Interact	Collaborate		
Open-source Software Stack	Pulser	Qadence	Solvers & Emulators			

HONEYWELL QUANTUM SOLUTIONS GENERATIONAL ROADMAP

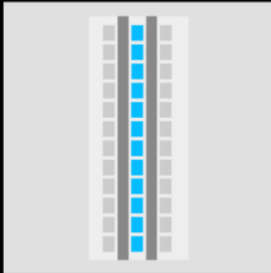
Noisy Intermediate-Scale Quantum (NISQ) Era

2030

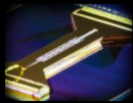
2020

Fault-Tolerant Quantum Computing

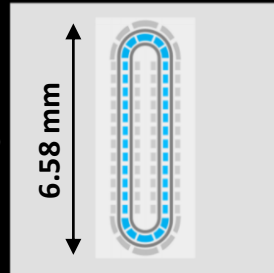
Model H1



Linear



Model H2



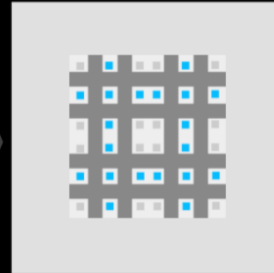
6.58 mm

Racetrack

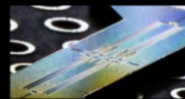


Multi-layer fab demonstrated

Model H3

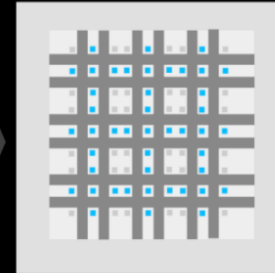


Grid

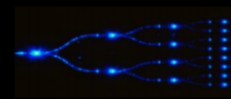


Junction transport demonstrated

Model H4

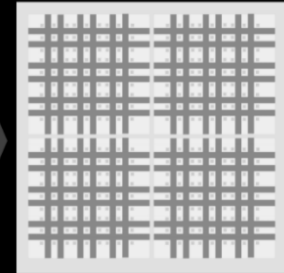


Integrated Optics

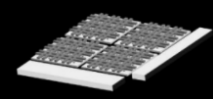


Photonic devices designed and tested

Model H5



Large Scale

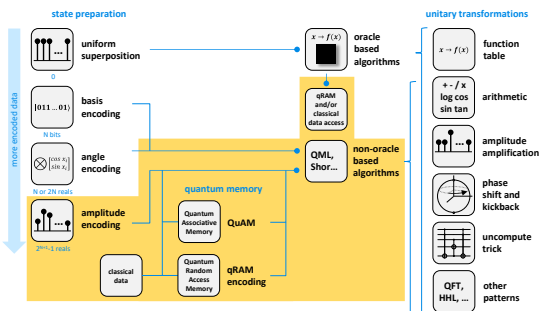


Ion-trap tiling strategy developed

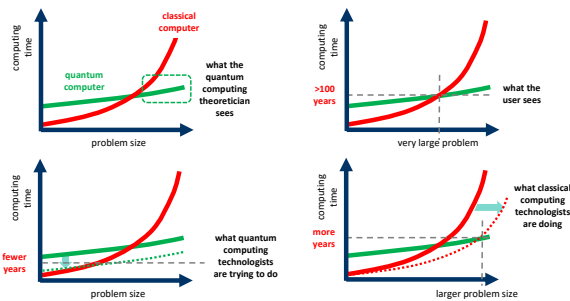
- 10 → 40 Qubits
- 2Q Fidelity: $\geq 99.5\%$
- All-to-all connectivity
- Conditional quantum logic
- Mid-circuit measurement
- Qubit reuse

- Massive scaling of physical qubits and computing power
- Ion trap fabrication in Honeywell's foundry
- Key enabling technologies already demonstrated for generational upgrades

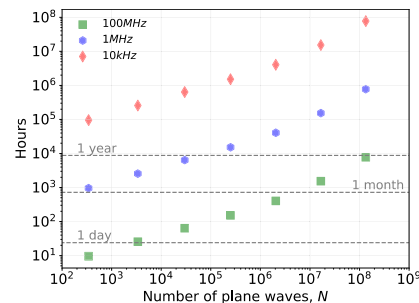
key software challenges



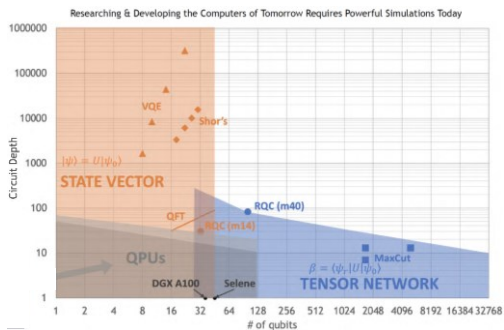
data loading



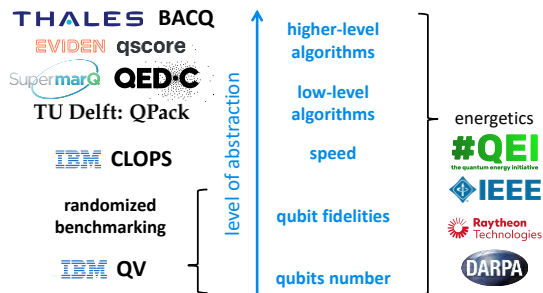
actual speedups



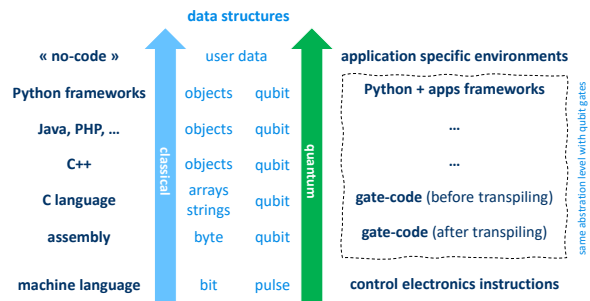
actual computing time



tensor networks competition

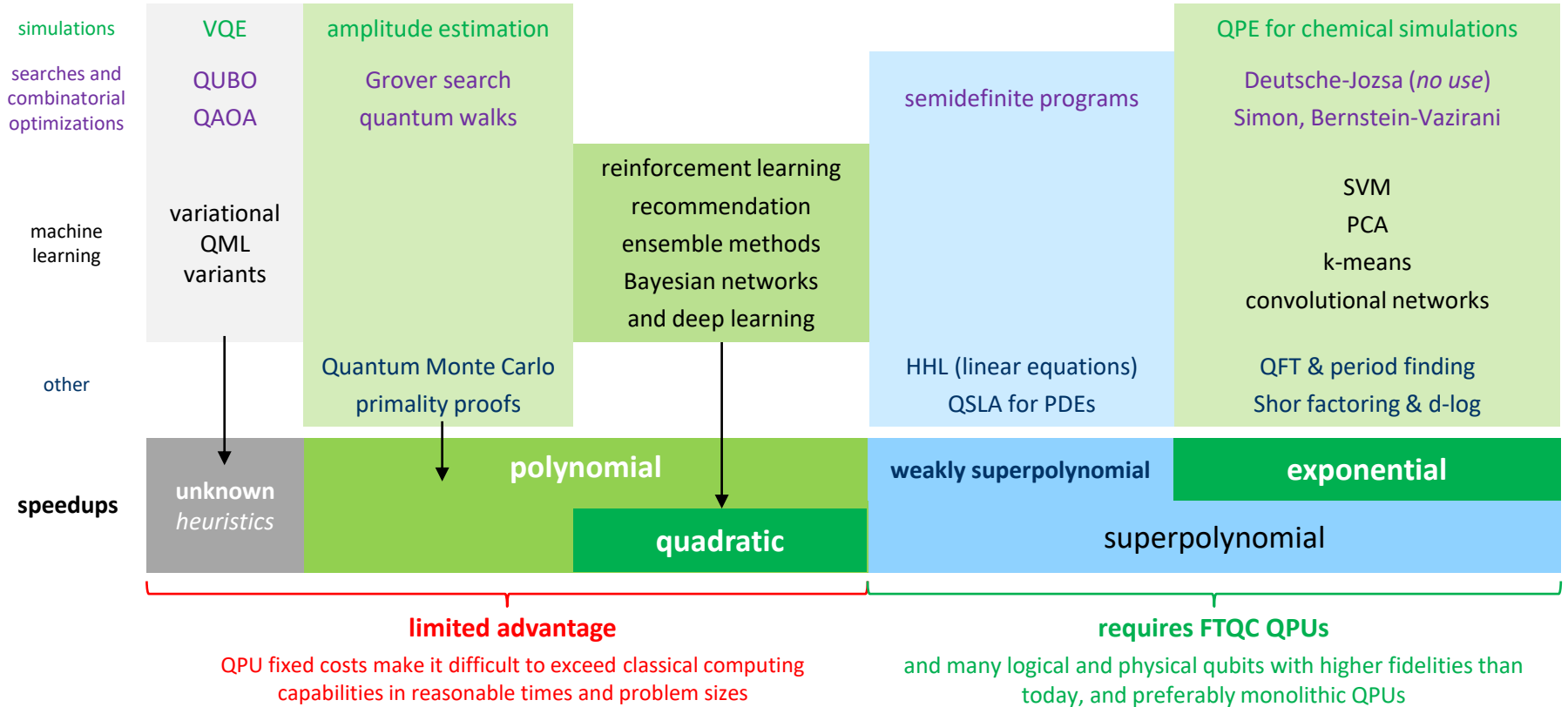


benchmarking

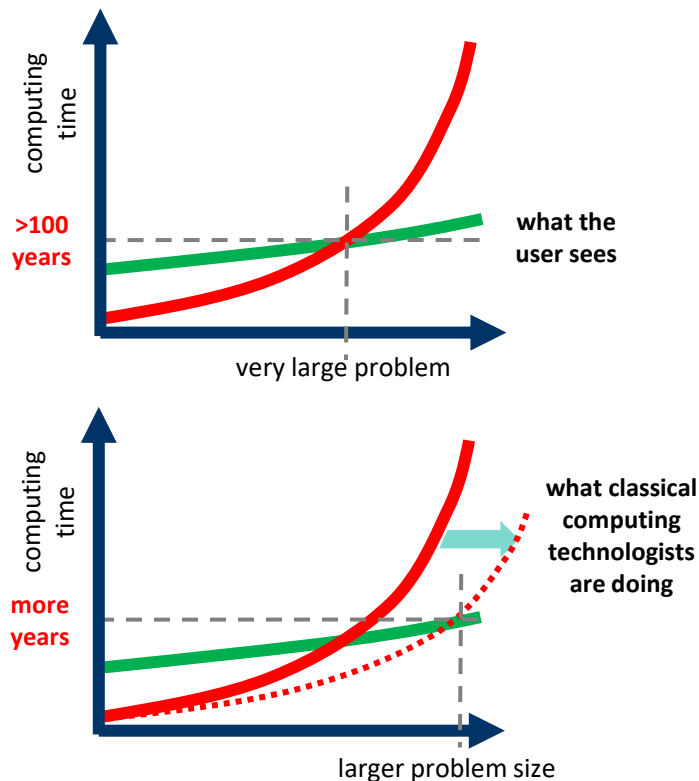
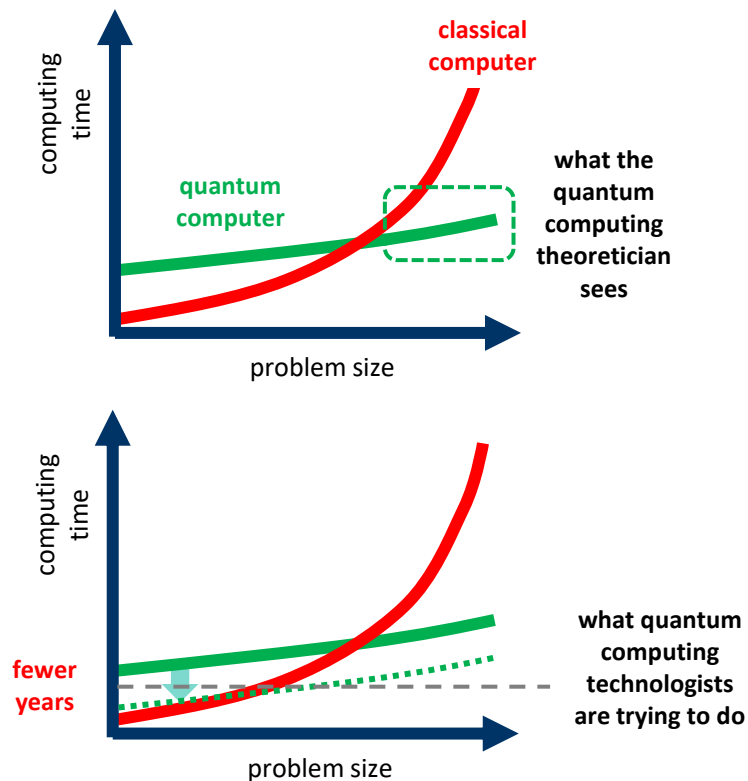


coding abstraction level

potential quantum speedups



a matter of perspective

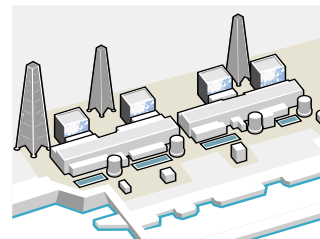
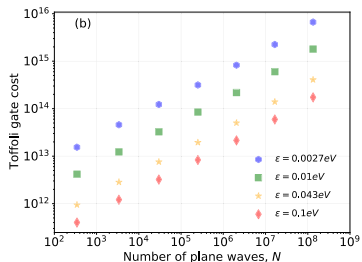
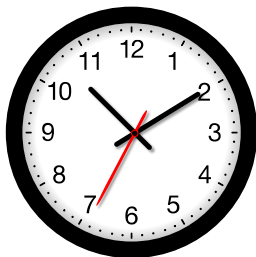


(cc) Olivier Ezratty, 2023, inspired by Disentangling Hype from Practicality: On Realistically Achieving Quantum Advantage by Torsten Hoefler, Thomas Häner, Matthias Troyer, 2023.

quantum advantages taxonomy

complex amplitudes of all combinations of 0 and 1

$\begin{bmatrix} \alpha_1 \\ \dots \\ \alpha_{2^N} \end{bmatrix}$	$ 00 \dots 00\rangle$
	$ 01 \dots 11\rangle$
	$ 11 \dots 11\rangle$



€ \$ £
TCO
ROI

space

the qubit register data space - scaling in 2^N complex numbers with N qubits - exceeds the memory capacity of classical computers.

speed

a quantum algorithm, including its classical part, runs faster than an equivalent best-in-class classical algorithms running on either the largest supercomputers or a given HPC configuration.

quality

the quality of the results of a quantum algorithm is better for some respect than the best-in-class classical algorithms. e.g: an error rate of a machine learning classification, a chemical simulation accuracy, or a better combinatorial problem solution.

energetic

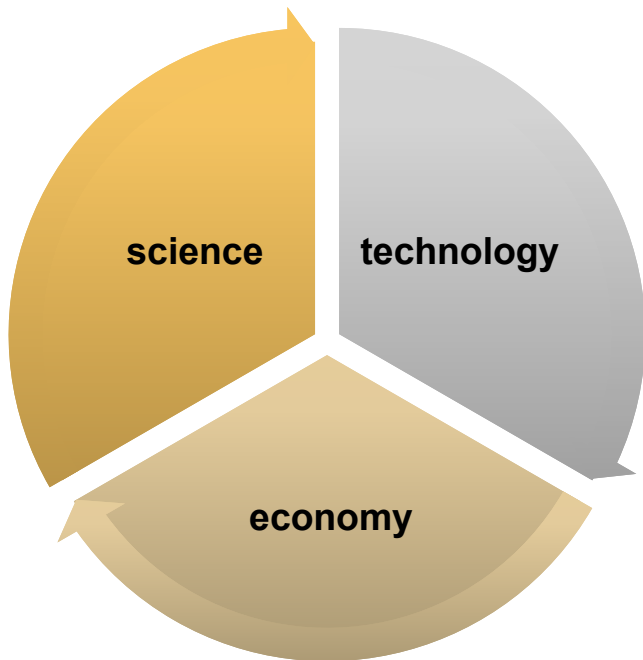
a fully-burdened quantum computer and algorithm configuration consumes less energy than the best-in-class classical equivalent.

cost

the total cost of the quantum solution is lower than the total cost of a best-in-class classical solution.

challenges ahead

- decoherence models
- noise models
- quantum control
- error correction codes
- cluster states creation
- qRAM
- QPU interconnect
- algorithms design
- complexity theory



- control electronics
- manufacturing quality
- cryogeny yield and power
- use cases
- software engineering
- emulators
- cloud infrastructure
- hybrid architectures
- benchmarking

- FPGA->ASIC
- VC, customer and governments investments
- fab investments
- other topics influences (LLMs, ...)

discussion



get the slides